

7. Transcriptional regulation from microarray data

Warning: Statistical physics.
It only works on average.

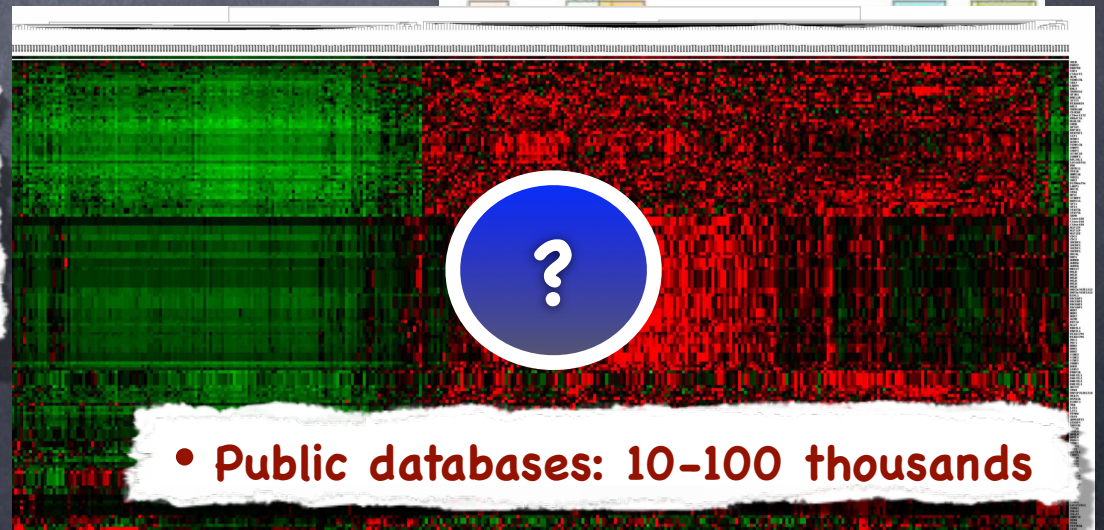
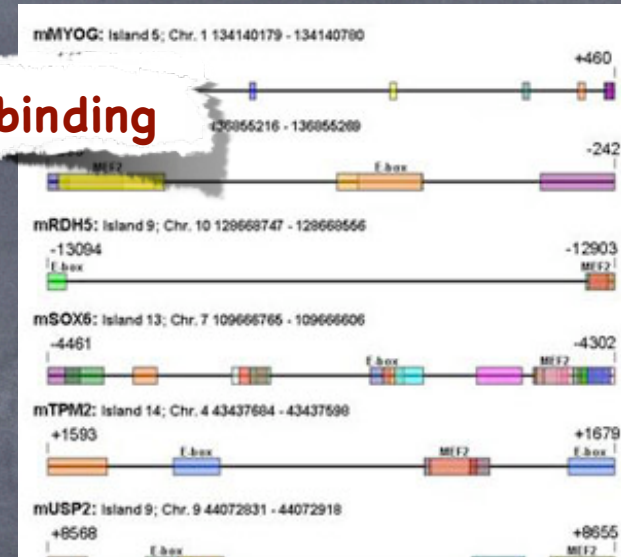
<http://regan.med.harvard.edu/CVBR-course.php>

How about the entire genetic regulatory network?



- Put together known literature
 - TRANSFAC, TRANSPATH
 - INGENUITY
 - InterAct

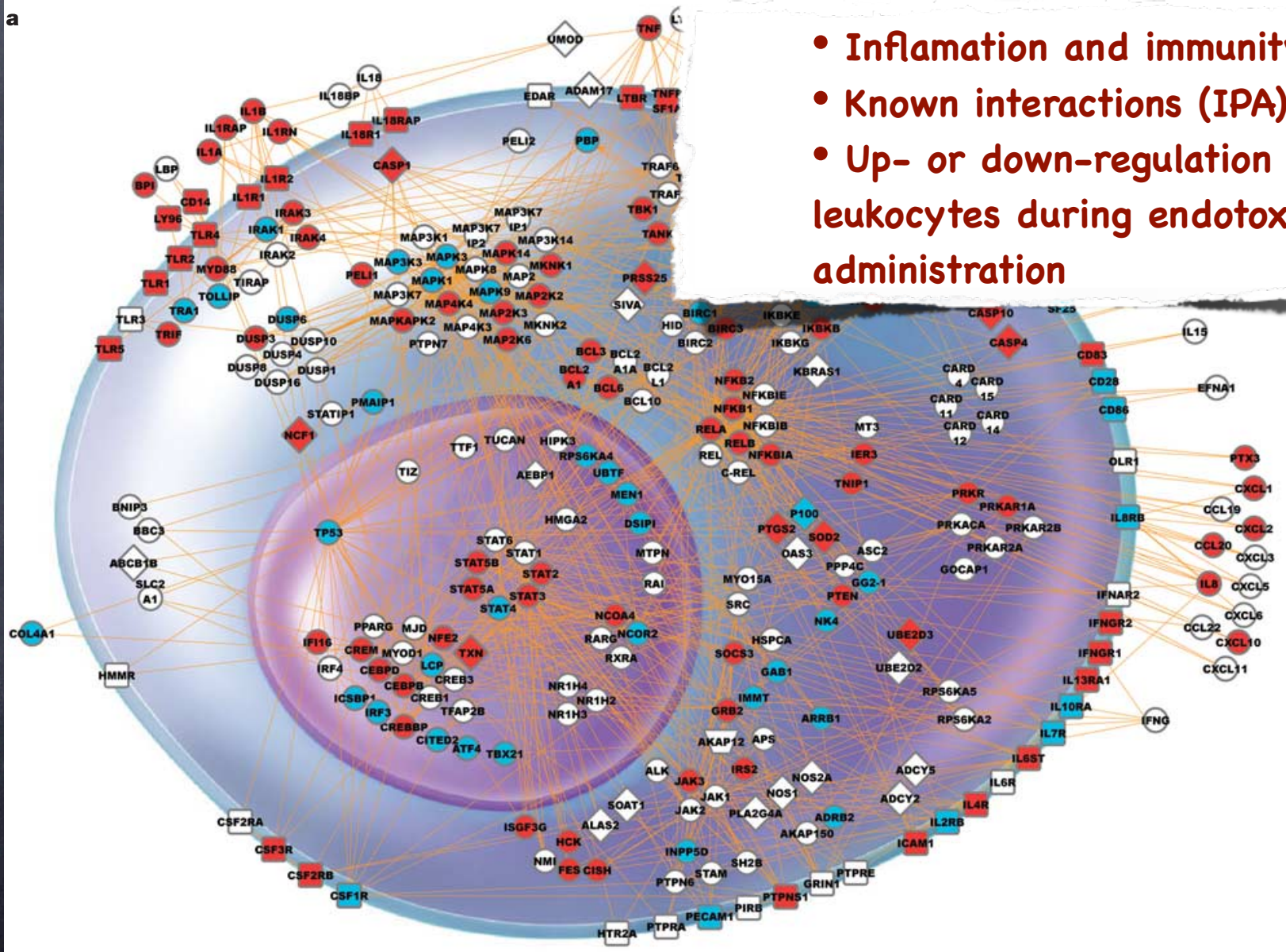
- Predict TF binding



- Public databases: 10-100 thousands

If we know enough interactions:

a



- Inflammation and immunity genes
- Known interactions (IPA)
- Up- or down-regulation in blood leukocytes during endotoxin administration

An overview of approaches

Co-expression networks

Boolean networks

ODEs and regression

Bayesian networks

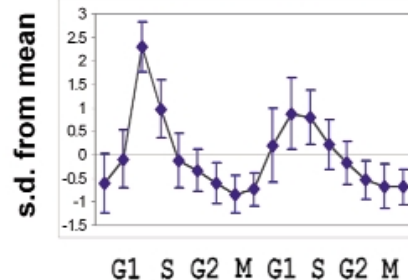
- Known literature
- Transcription factors
- Binding site information
- Perturbation experimental design

How far does correlation take us?

- Hypothesis: co-expression means
 - common upstream regulator
 - shared function

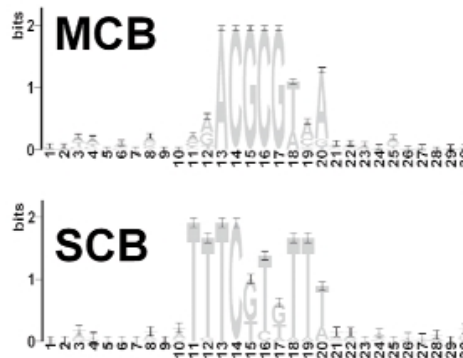
Common TF binding site specific to this cluster

replication & DNA synthesis (2)

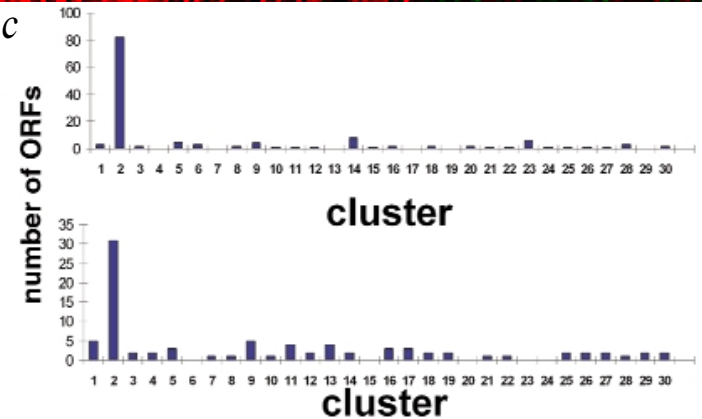


Yeast

b



c



Sounds nice! How does clustering go?

- Data preparation & normalization

All capture functionally related gene groups

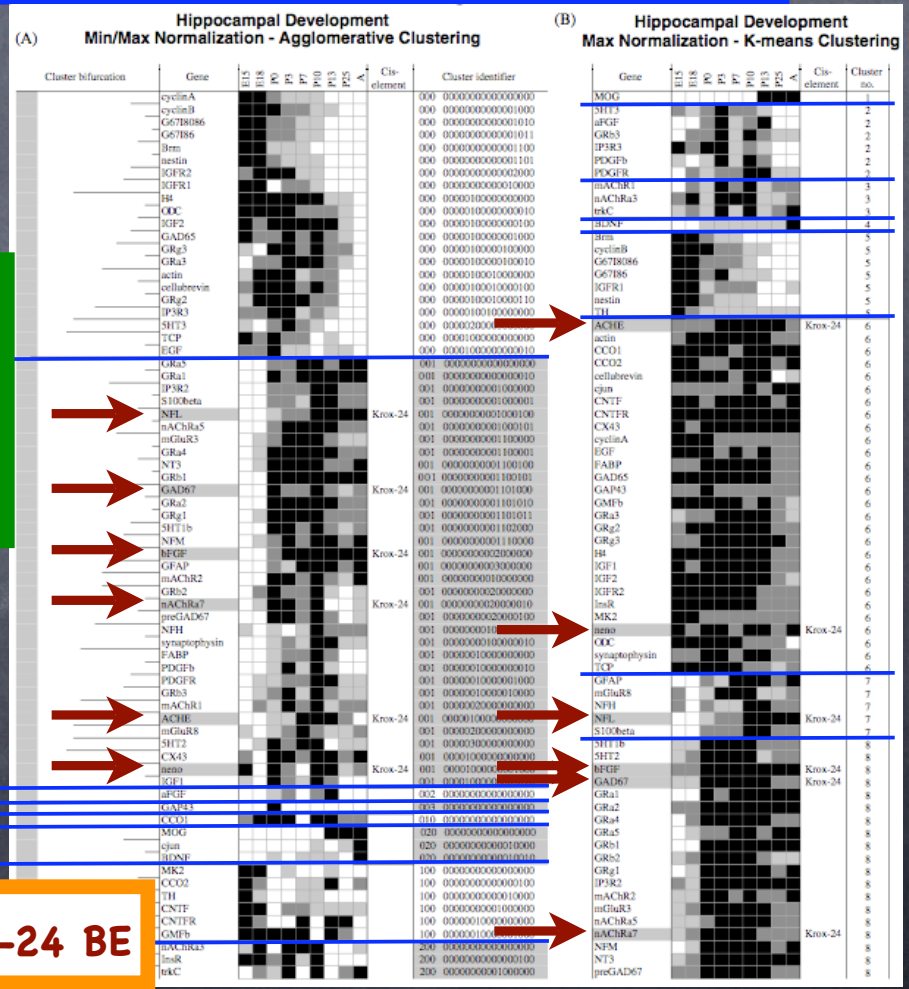
- A distance metric: what does "similar" mean?

Different results on the same dataset

- Pearson correlation
- Eukclidean distance
- Mutual Information
- ...

- Clustering
 - Hierarchical
 - Non-hierarchical
 - K-means
 - SOM
 - PCA
 - Fuzzy clustering
 - ...

No consensus on which one is better (no metric for "better")

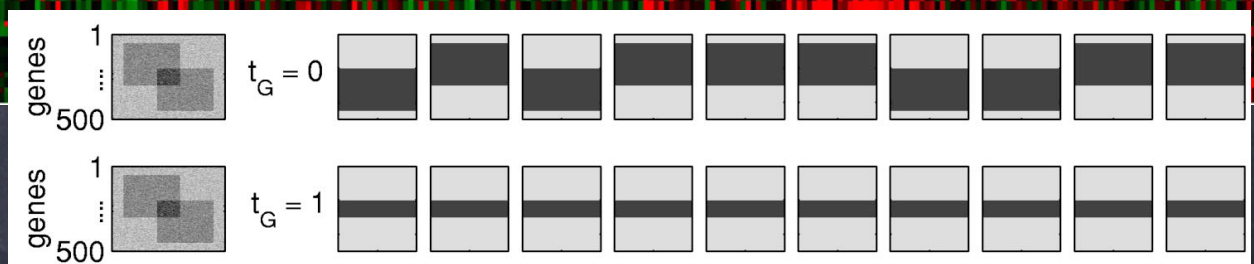


Rat, Krox-24 BE

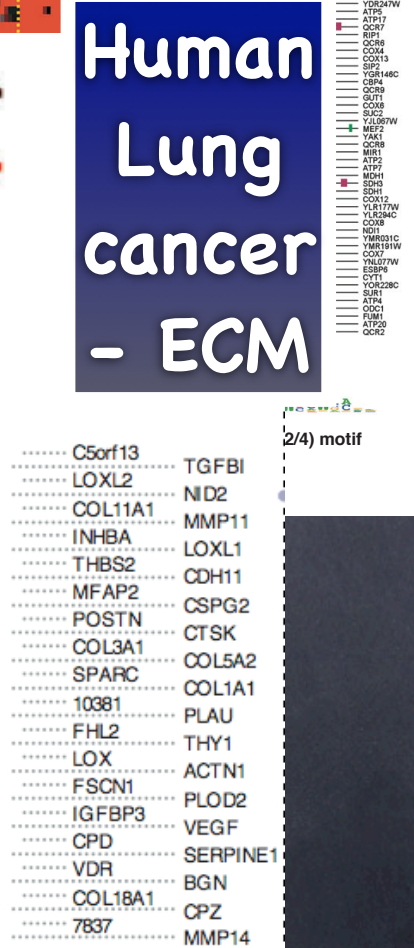
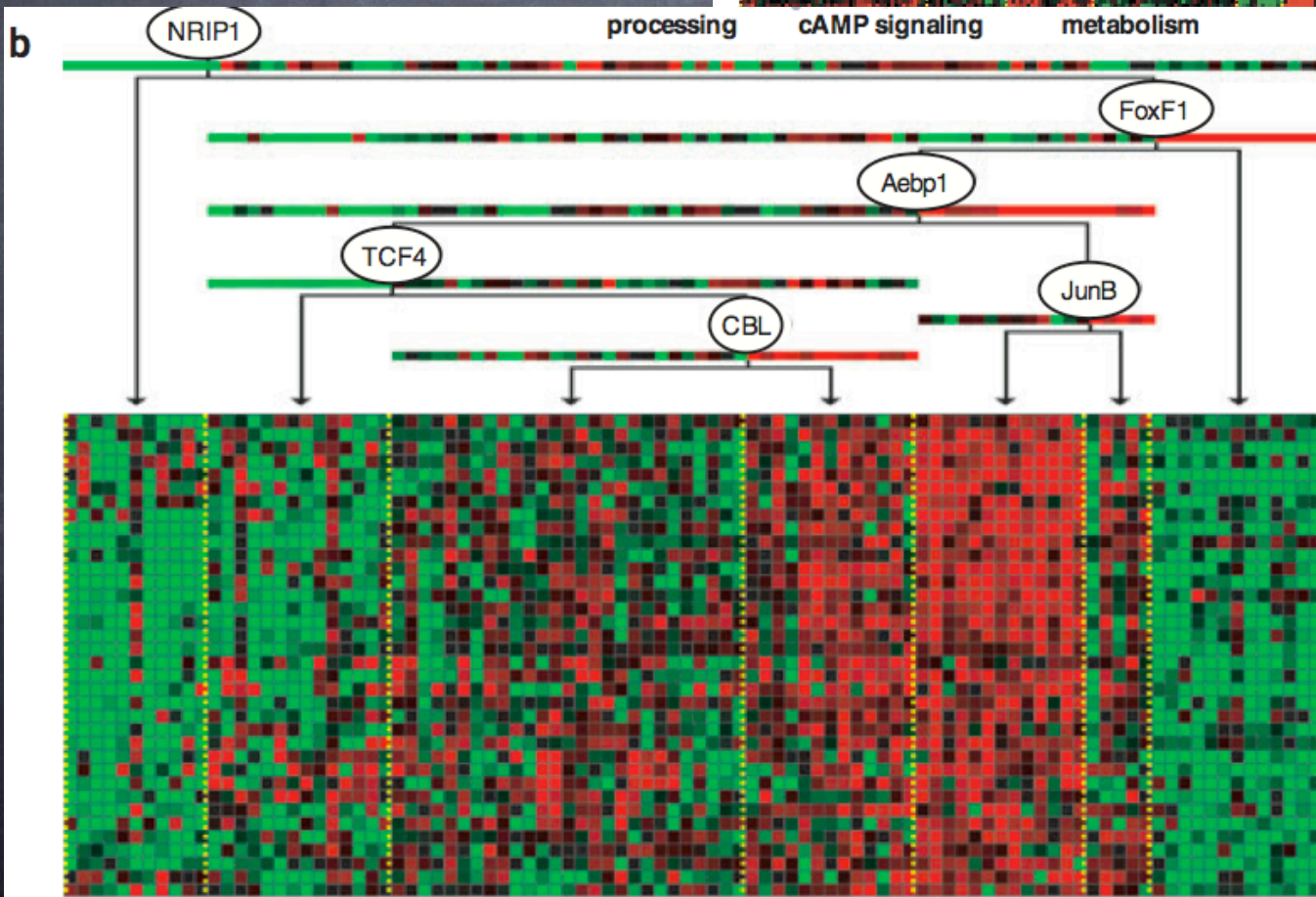
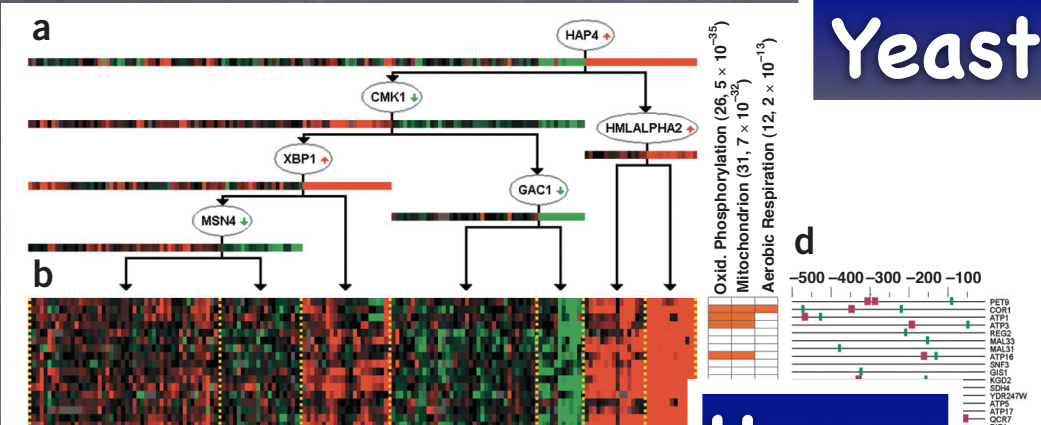
Coherent groups of genes & experiments

Ideally, all combinations of genes & experiments should be tested

- Iterative Signature Algorithm

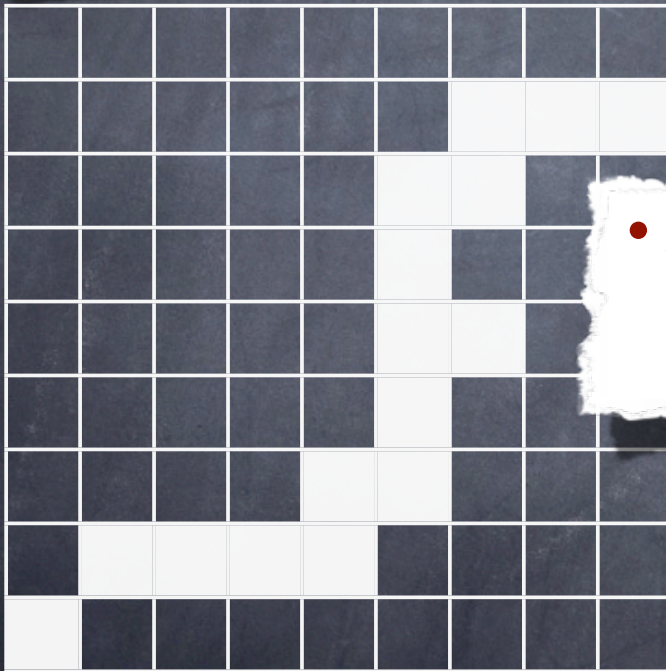


Regulators with best predicting power



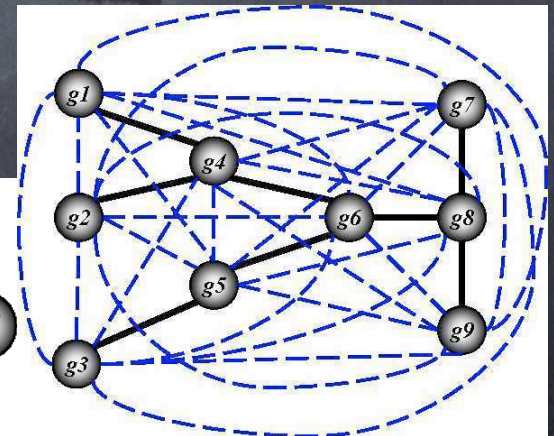
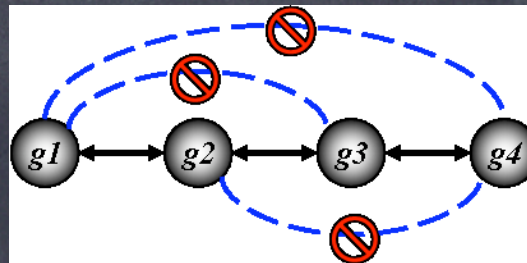
Does correlated behavior translate to direct regulation?

- **Mutual Information**
 - non-linear measure of correlated behavior



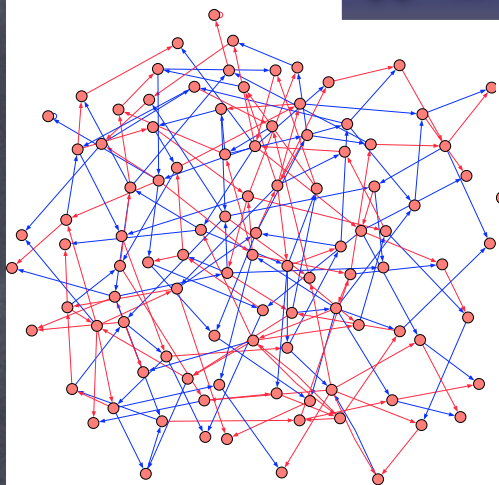
$$I(X; Y) = \sum_{y \in Y} \sum_{x \in X} p(x, y) \log \left(\frac{p(x, y)}{p_1(x) p_2(y)} \right)$$

- **ARACNE**
 - Mutual Information
 - Data processing inequality

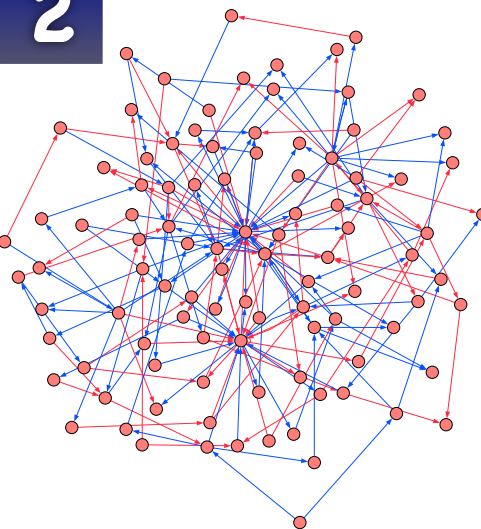


Test of ARACNE

$k = 2$

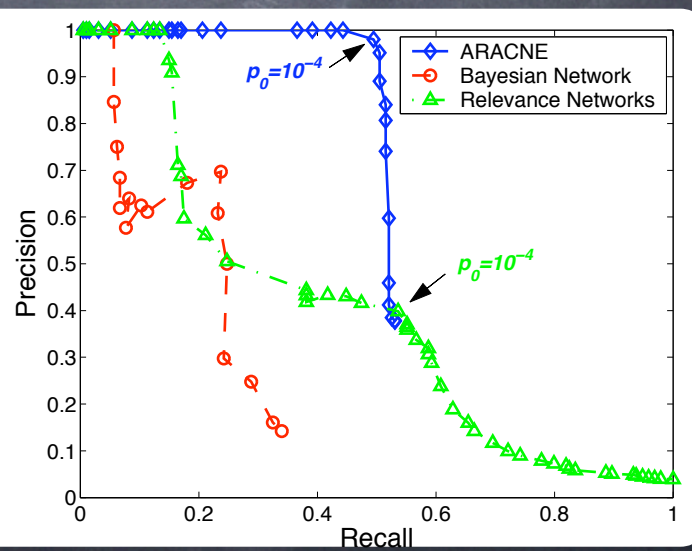
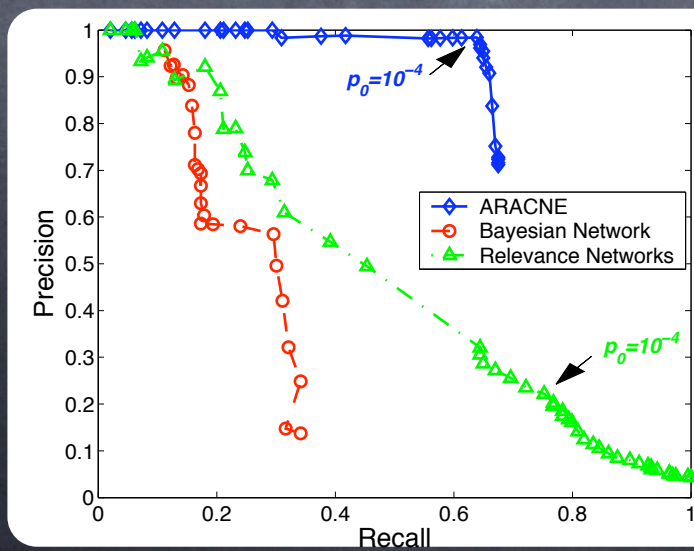


Erdos-Renyi

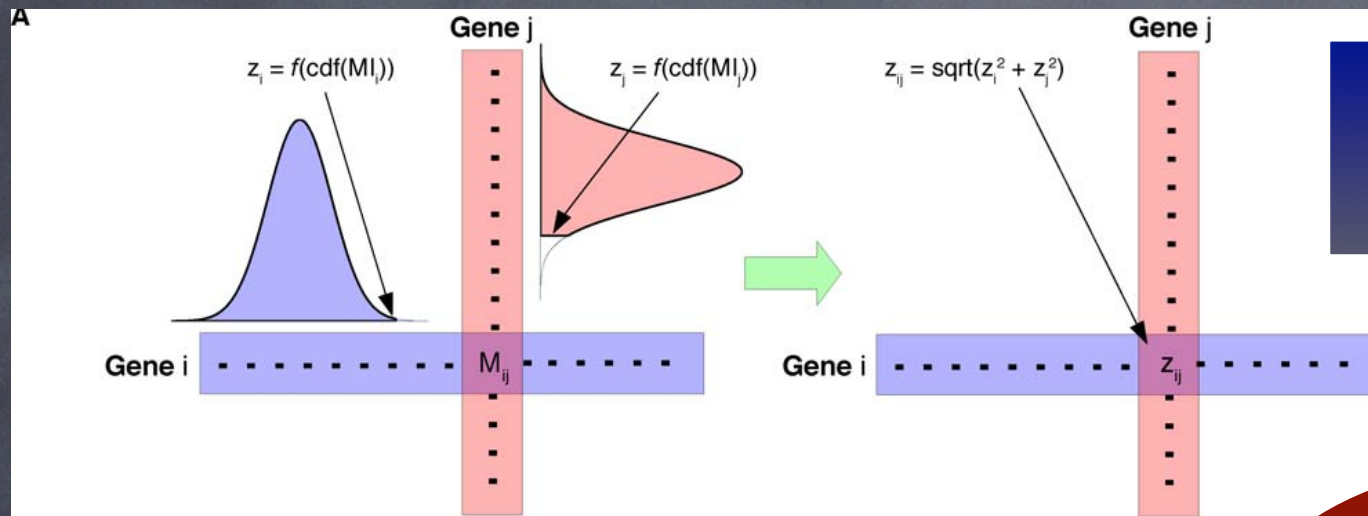


Barabasi-Albert

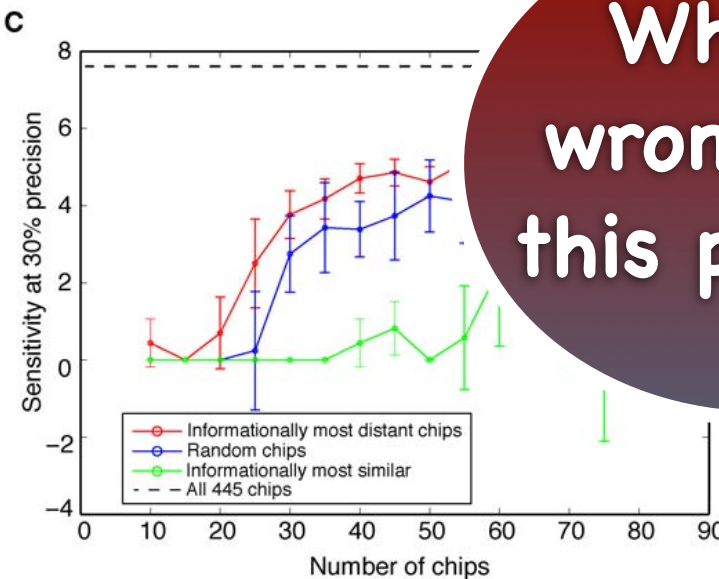
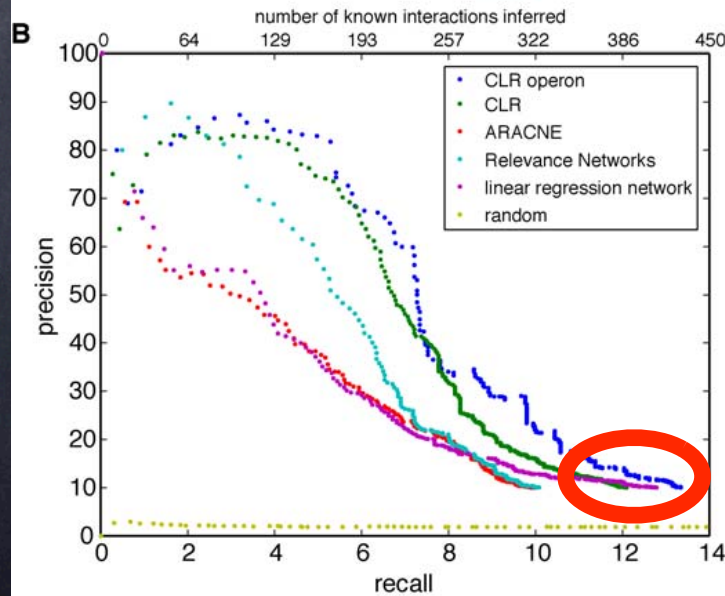
How about real microarray data?



CLR - Context Likelihood of Relatedness

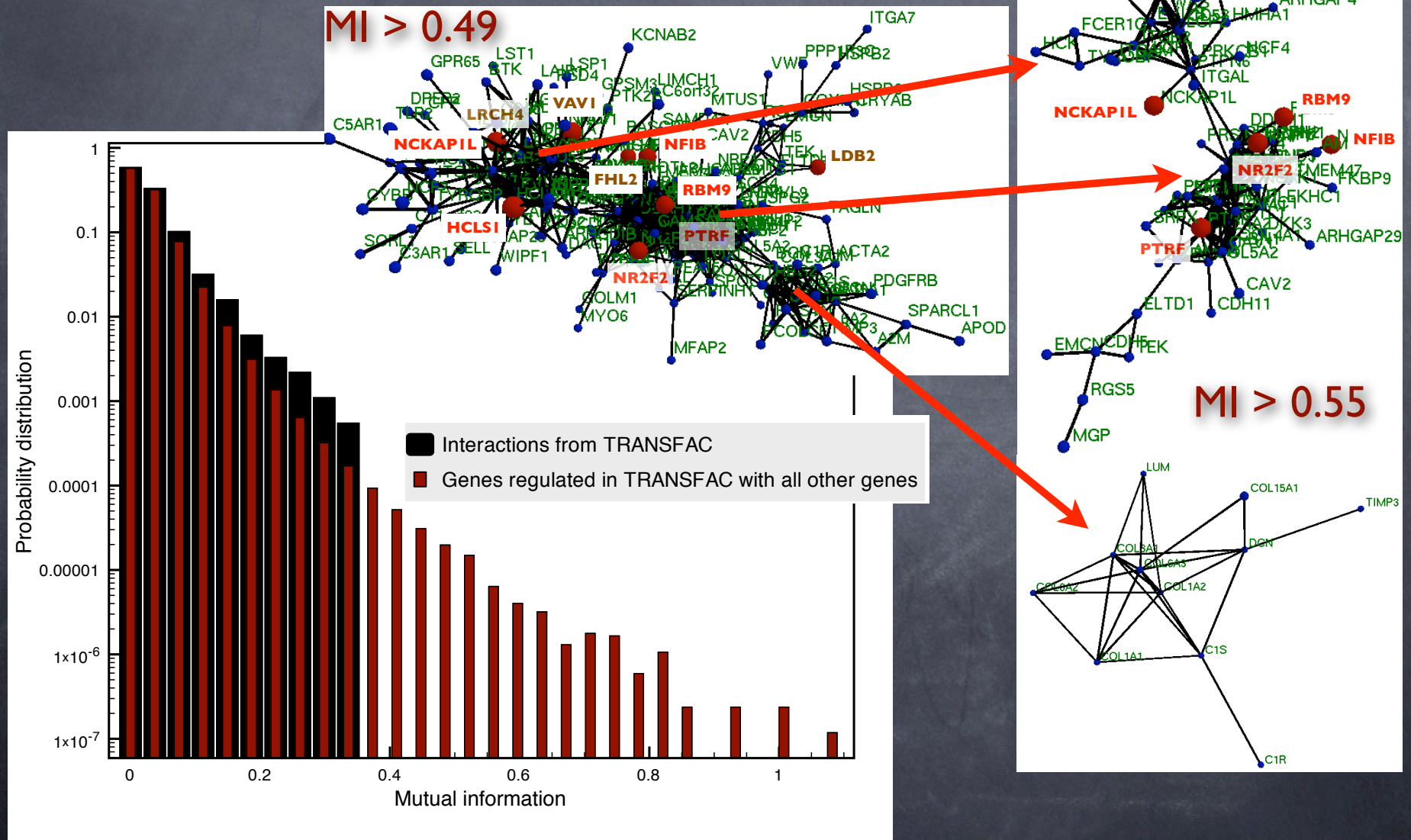


TF → G
only



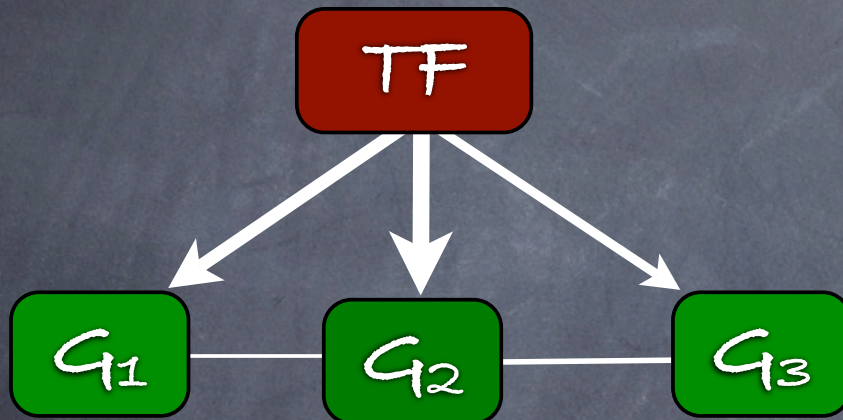
What is wrong with this picture?

Co-expression is strongest between co-regulated genes!

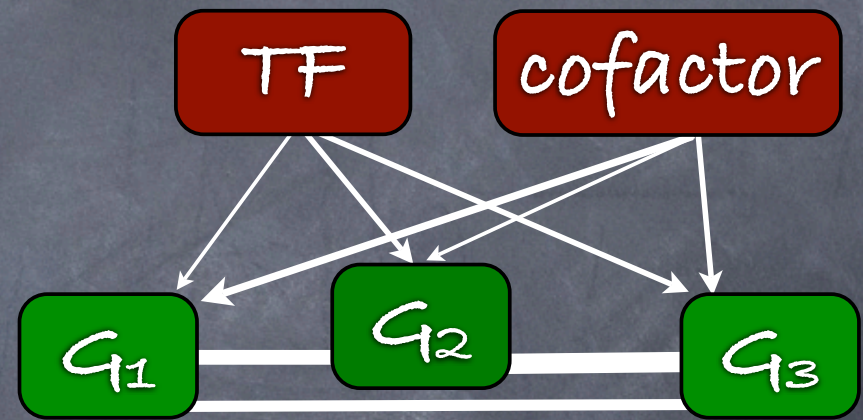


Reasons behind the trouble

- ARACNe **IFF**
1 input/ gene!



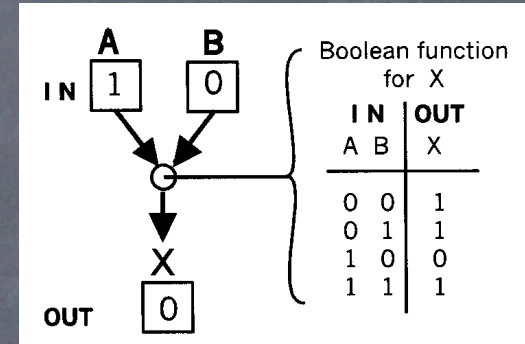
- Fails for combinatorial regulation



Is direct regulatory information contained in MA data?

Boolean network approaches

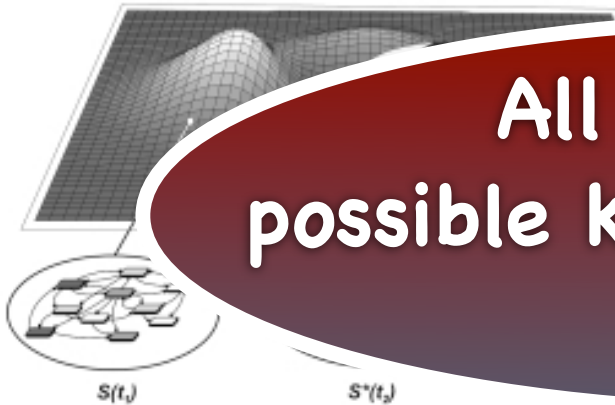
- State of the system, or gene activity profile: $(0,1,1,0,0,1,1,1,0,\dots,0)$
- State changes in time: trajectory in nD space
- Structure of state space determines all possible dynamics



* Ordered systems

- Only a small fraction of all cell states are stable
- The system does not visit all possible states
- **Attractors:**

C high-dimensional system as "attractor landscape (schematic)



All genes ← all possible k inputs need to be tested

points: a state in which all constraints are satisfied
 the number of states in which the constraints are satisfied

attractor basins

Finding expression dependencies

- Bayesian networks
 - Directed Acyclic Graph
 - Its structure describes the conditional probabilities that best fit the data
 - Discrete or continuous
 - Extremely time-consuming on large networks

- Regression based methods

$$X_i^{(k)} = \sum_j h_{j \rightarrow i} \cdot X_j^{(k)} + p_i^{(k)}$$

$$N_{\text{exp}} \ll N_{\text{gene}}$$

1: Maximum k inputs / gene

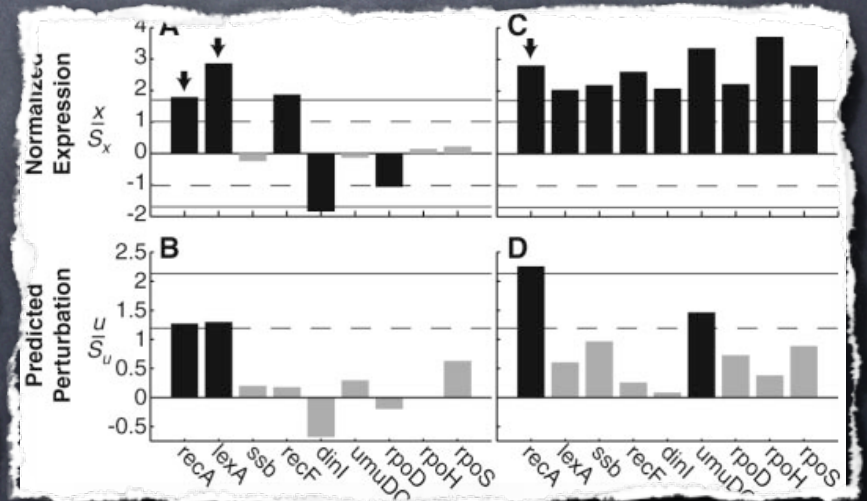
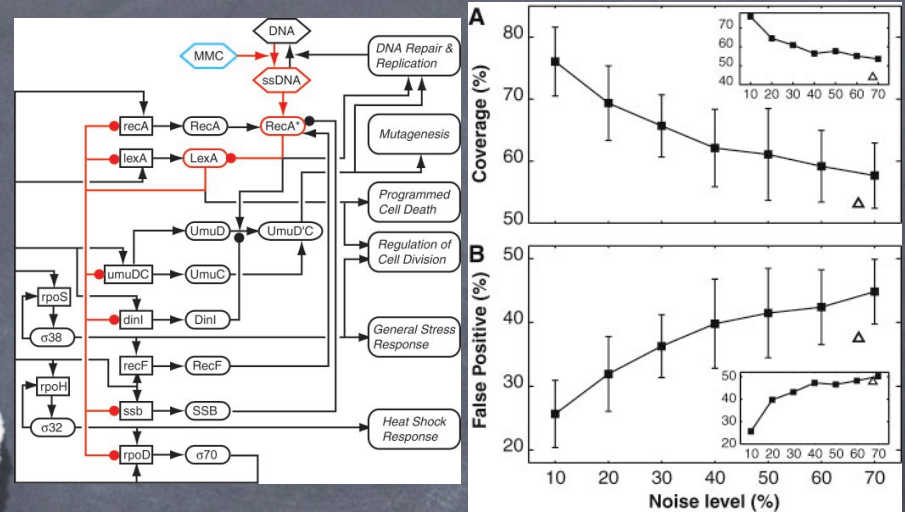
2: Find relevant part of gene space

NIR - Network identification by Multiple regression

$$X_i^{(k)} = \sum_j h_{j \rightarrow i} \cdot X_j^{(k)} + p_i^{(k)}$$

$$\sum Z_j^{(k)} \cdot A'_{ji} = -P_i^{(k)}$$

- Iterative approximation
 - 0^{th} approximation:
 - calculate $P_i^{(k)}$
 - for each gene
 - use $n \in (Q, M)$ equations where $p_i < p_c$
 - solve



Summer break!

Next lecture:

Sep 14

12 PM