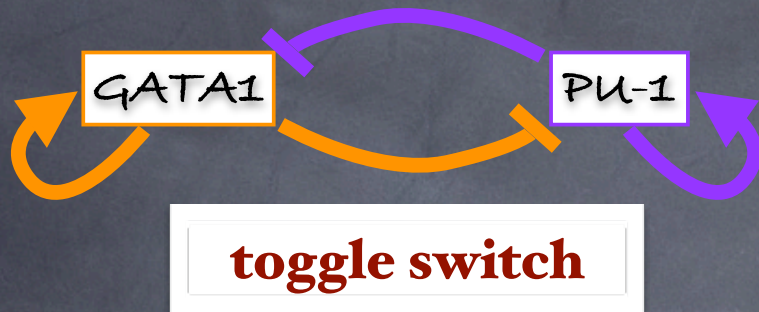


# 5. Regulatory Models that Mimic Phenotype and Dynamics, Part I

Warning: Statistical Physics.  
It only works on average.

<http://regan.med.edu/CVRB-course.php>

# Multi-stable circuits



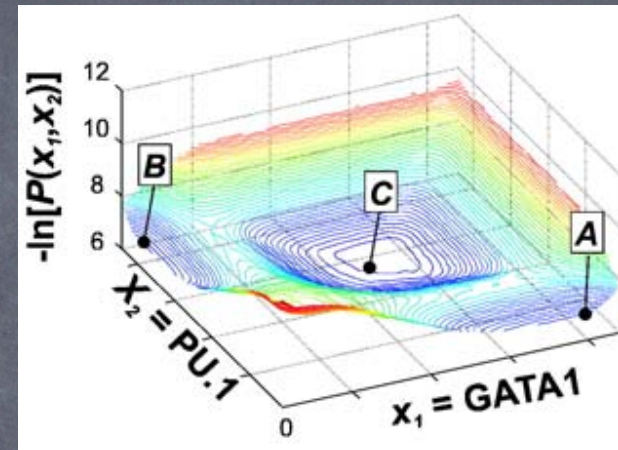
- The simplest “developmental” type circuit
- Bistable

- Modeling

- ➔ differential equations
- ➔ Gillespie stochastic dynamics
- ➔ Thermodynamic models of binding and transcription
  - ➔ concentration dependence
  - ➔ precise dynamics of switching

- Boolean dynamics

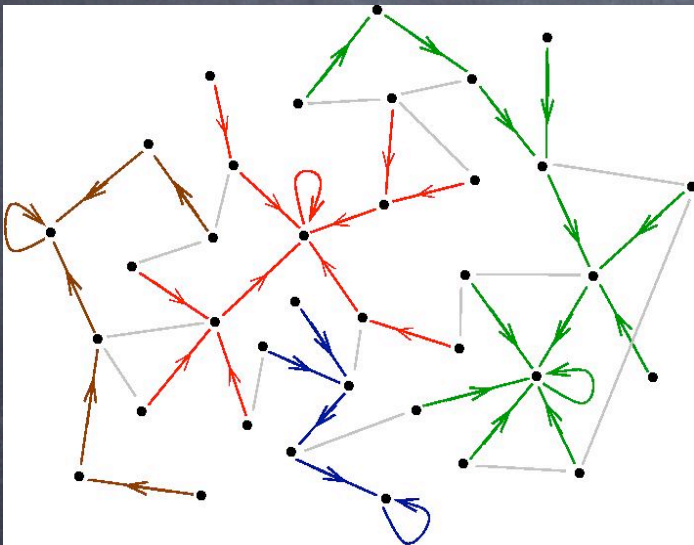
- ➔ logic gates
- ➔ discrete time
- ➔ captures broad-scale features



GATA1	PU-1	GATA1	PU-1
ON	ON	OFF	OFF
ON	OFF	ON	OFF
OFF	ON	OFF	ON
OFF	OFF	ON	ON

# Boolean networks

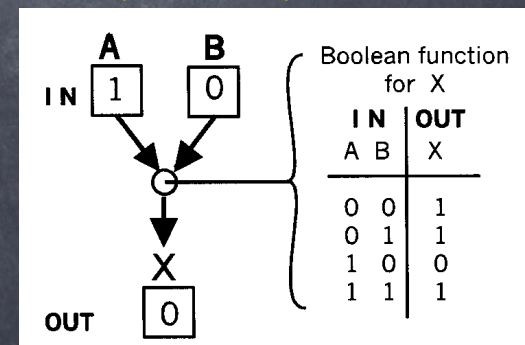
Kauffman, S, Homeostasis and differentiation in random genetic control networks  
Nature 224, pp 177, 1969



- Random network
- State of the system, or gene activity profile:  $(0,1,1,0,0,1,1,1,0,\dots,0)$
- Random Boolean rules
  - $p$  – prob. output value 1

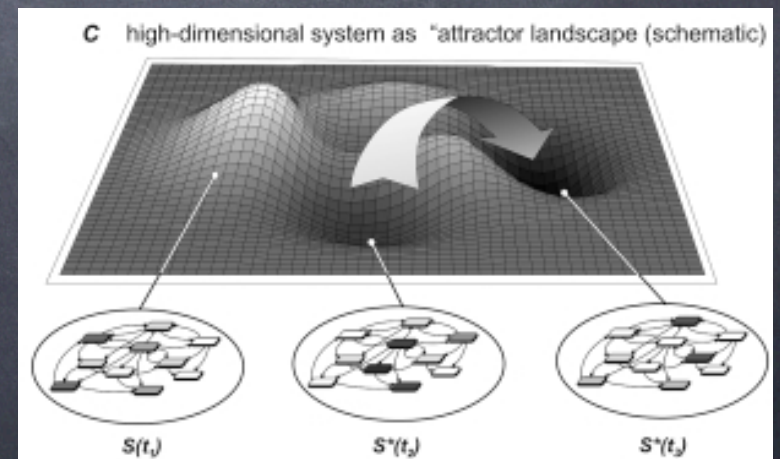
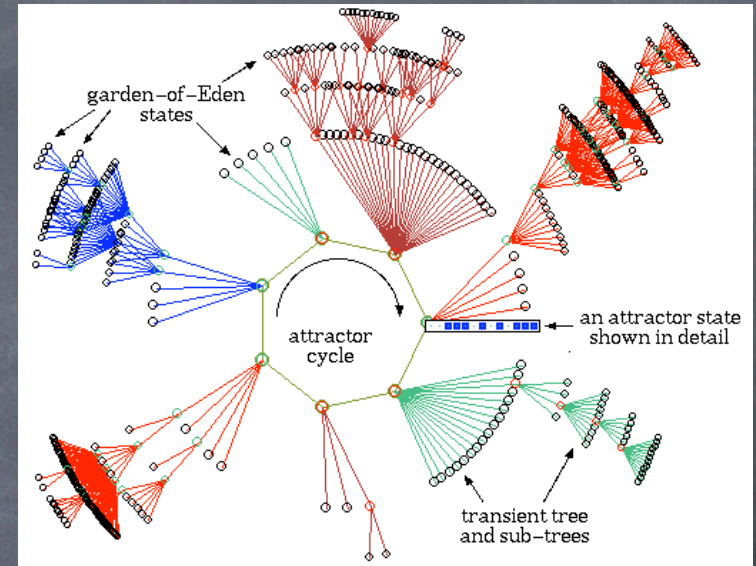
- State changes in time: trajectory in  $nD$  space
- **Structure of state space determines all possible dynamics**

(NOT A) OR B



# Random Boolean networks have an ordered regime

- Only a small fraction of all cell states are **stable**
- The system does not visit all possible states
- **Attractors:**
  - Fixed points: a state in which all Boolean rules are satisfied
  - Limit cycles: a finite number of states through which the system cycles
- **Attractor basins**

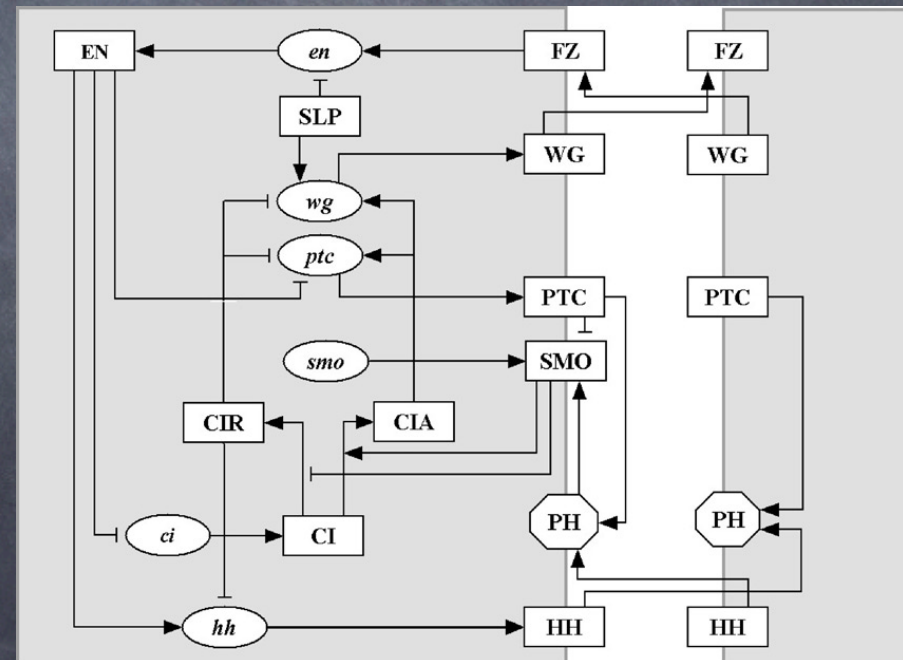
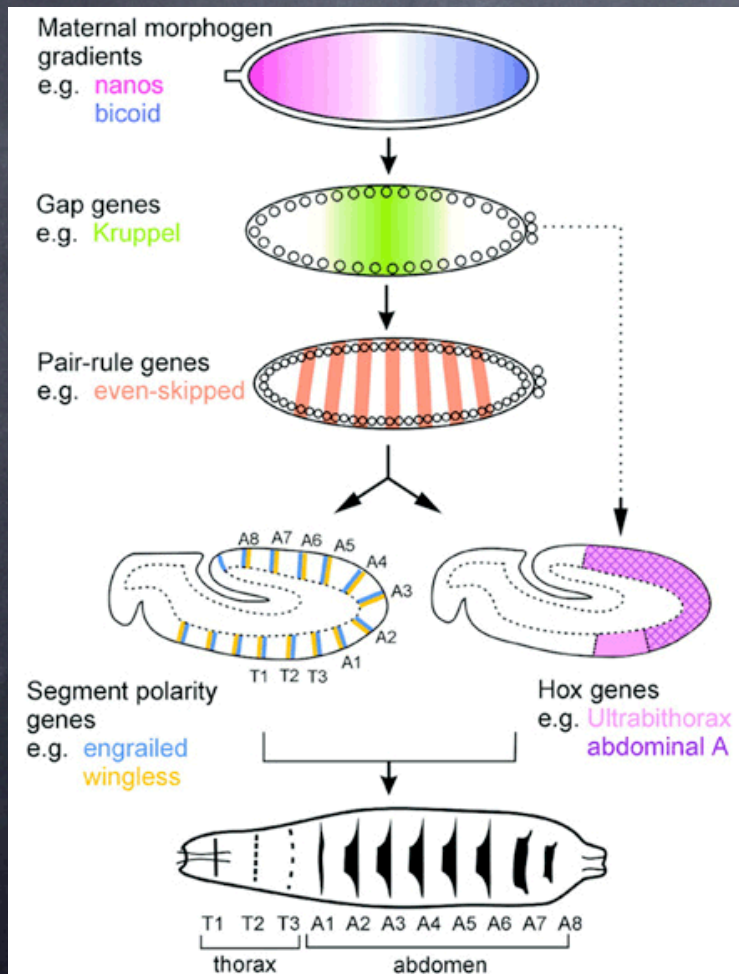


# Physicists love this. Biology... not so much

“Random” is not a good interdisciplinary word.

Reka Albert & Hans G. Othmer

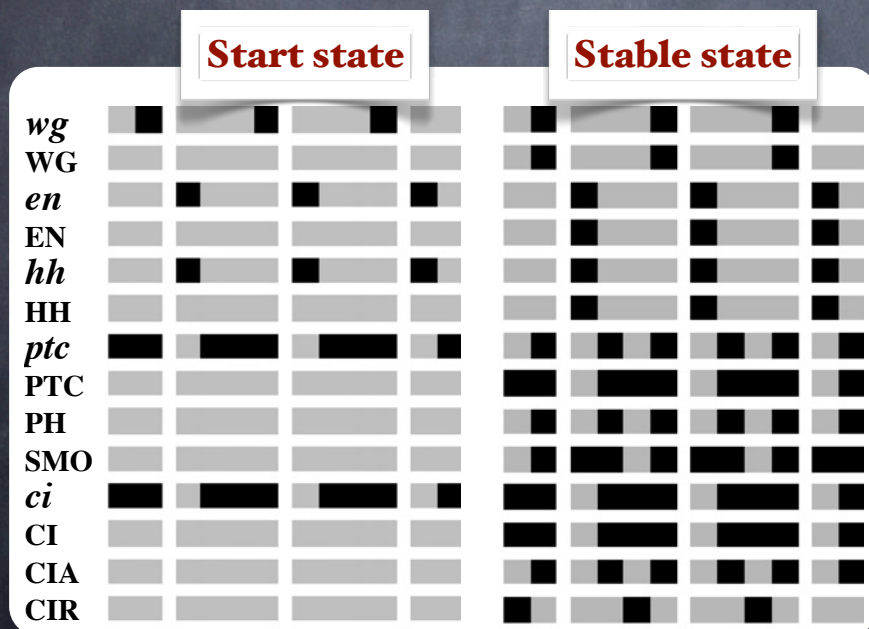
## Drosophila segment polarity network



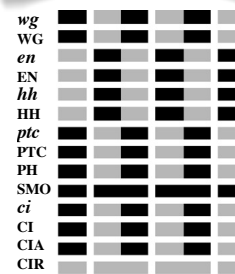
# Boolean rules and correct topology are sufficient!

- The network topology was known, most Boolean rules could be inferred from literature
- Small enough system for exact enumeration!

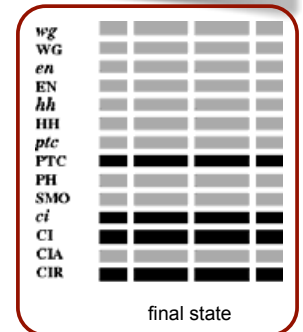
- (i) the effect of transcriptional activators and inhibitors is never additive, but rather, inhibitors are dominant;
- (ii) transcription and translation are ON/OFF functions of the state;
- (iii) if transcription/translation is ON, mRNAs/proteins are synthesized in one time step;
- (iv) mRNAs decay in one time step if not transcribed;
- (v) transcription factors and proteins undergoing post-translational modification decay in one time step if their mRNA is not present.



## Heat shock

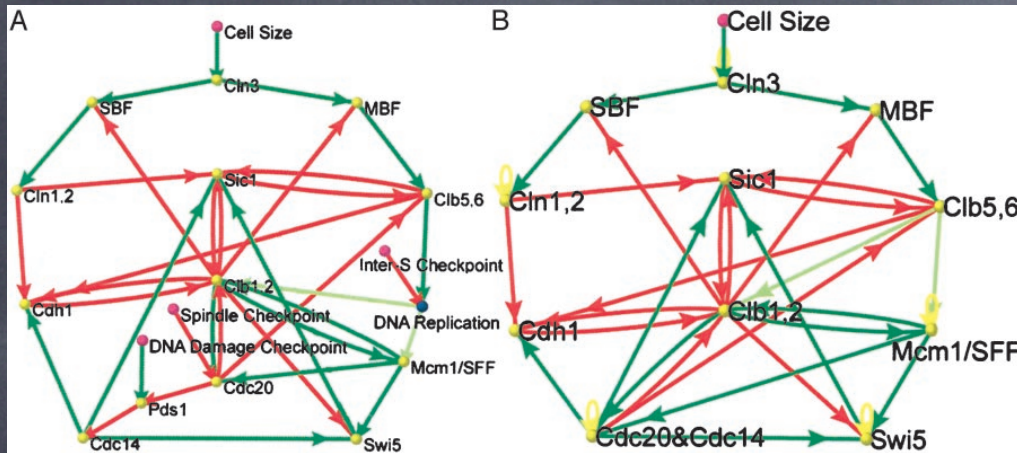


## Lethal mutants ( $\sim wg, en, hh$ )



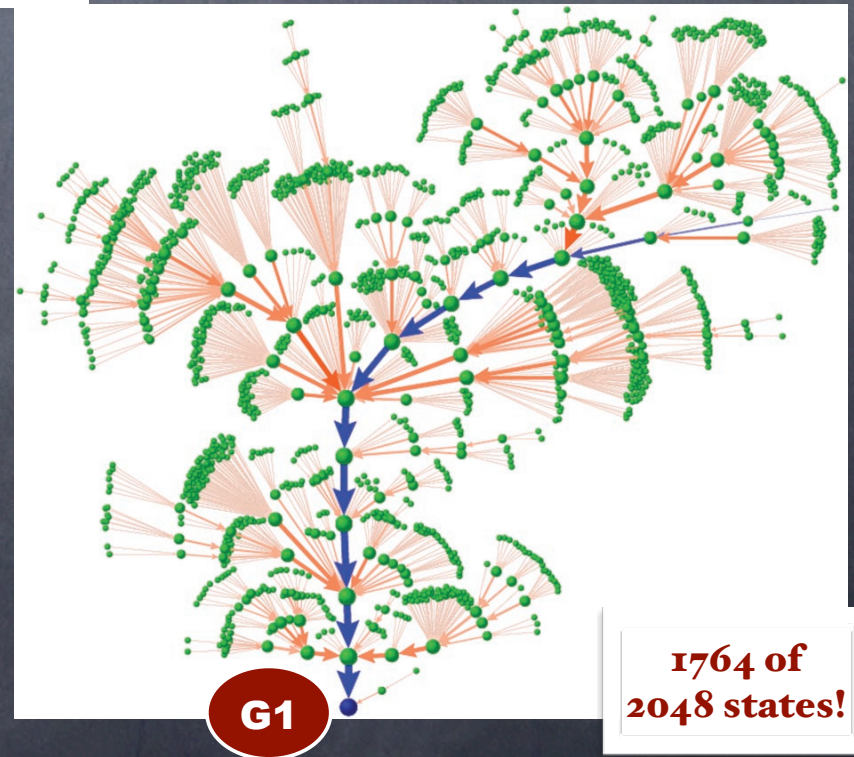
No *wg*, *en* and *hh* stripes, no segmentation, regardless of initial state.

# The yeast cell cycle



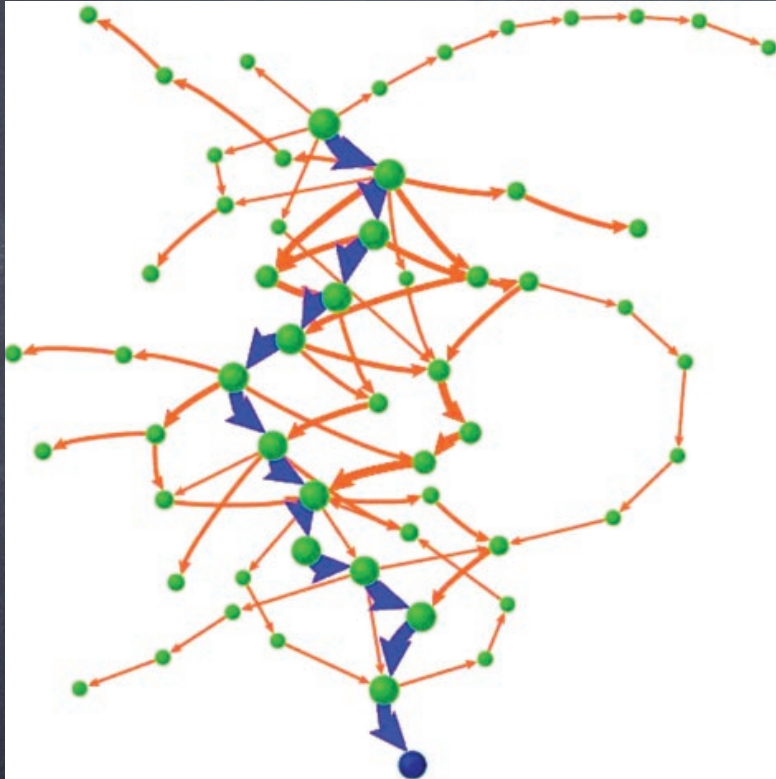
- The network topology is known
- **NO Boolean rules, just activator/inhibitor relationships**

$$S_i(t + 1) = \begin{cases} 1, & \sum_j a_{ij} S_j(t) > 0 \\ 0, & \sum_j a_{ij} S_j(t) < 0 \\ S_i(t), & \sum_j a_{ij} S_j(t) = 0 \end{cases}$$



**1764 of  
2048 states!**

# Robust in more than one way



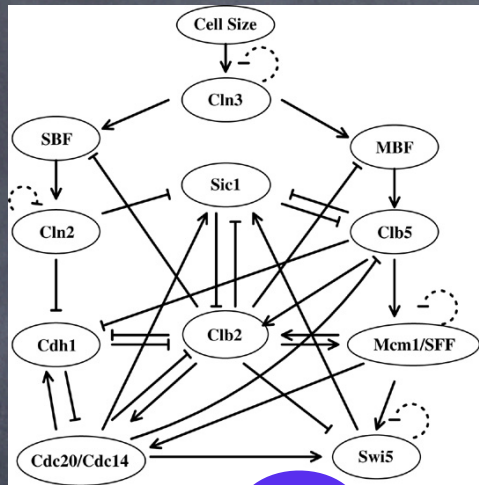
- Dynamics under perturbation
  - start dynamics from START
  - superimpose time-course for perturbed networks
    - ➔ 34 arrow deletions (41%)
    - ➔ 174 arrow additions (57%)
    - ➔ 29 activator/inhibitor switch (68%)

- Similar stable fixed point with
  - ➔ different dynamical rules
  - ➔ using other checkpoints



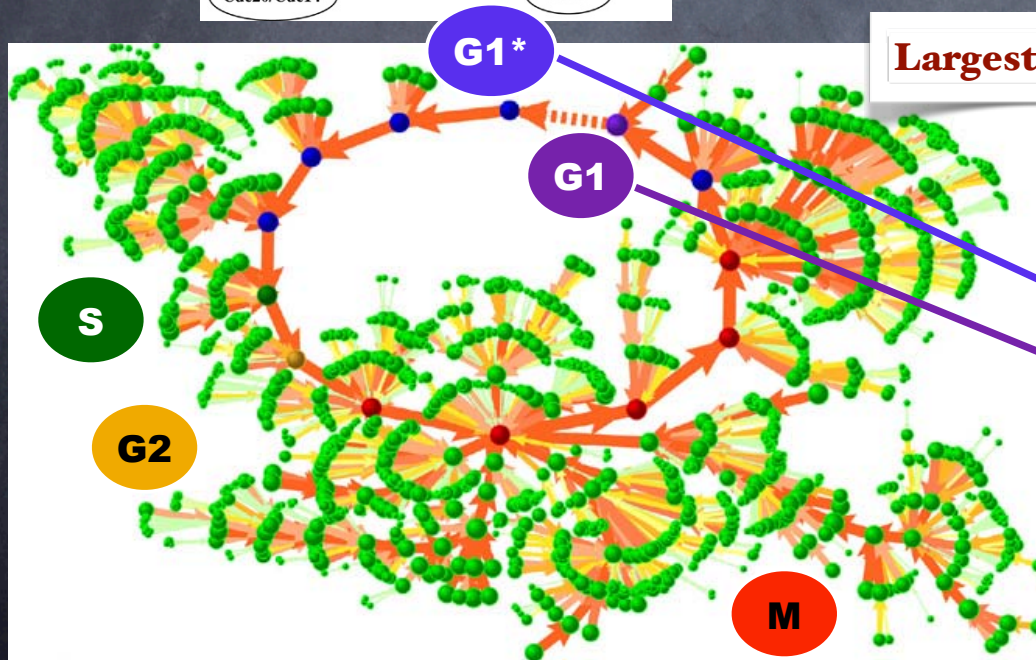
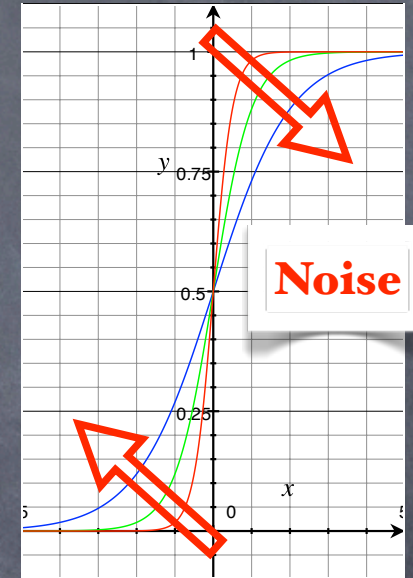
# How about noise?

- Probabilistic cell cycle network



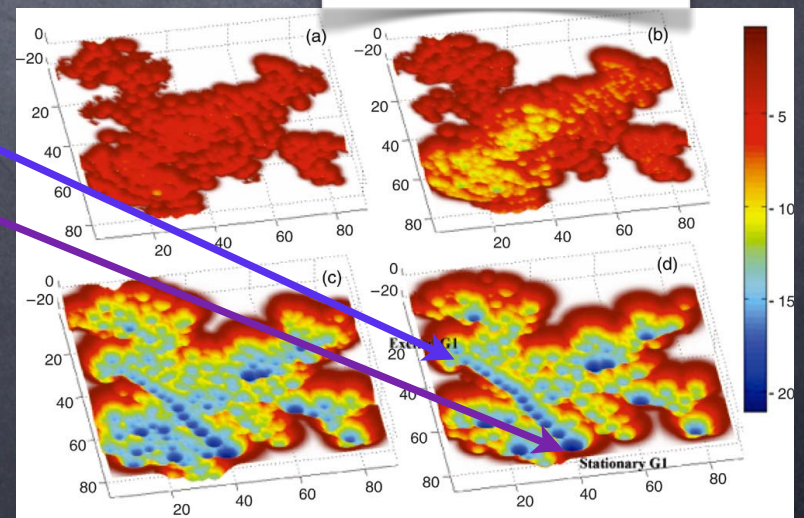
$$P_r(s_i(t+1) = \sigma_i \mid s_1(t), \dots, s_{11}(t)) = \frac{\exp(\beta(2\sigma_i - 1)T)}{\exp(\beta T) + \exp(-\beta T)}$$

if  $T = \sum_{j=1}^{11} a_{ij}s_j(t) \neq 0, \sigma_i \in \{0, 1\}$ ;



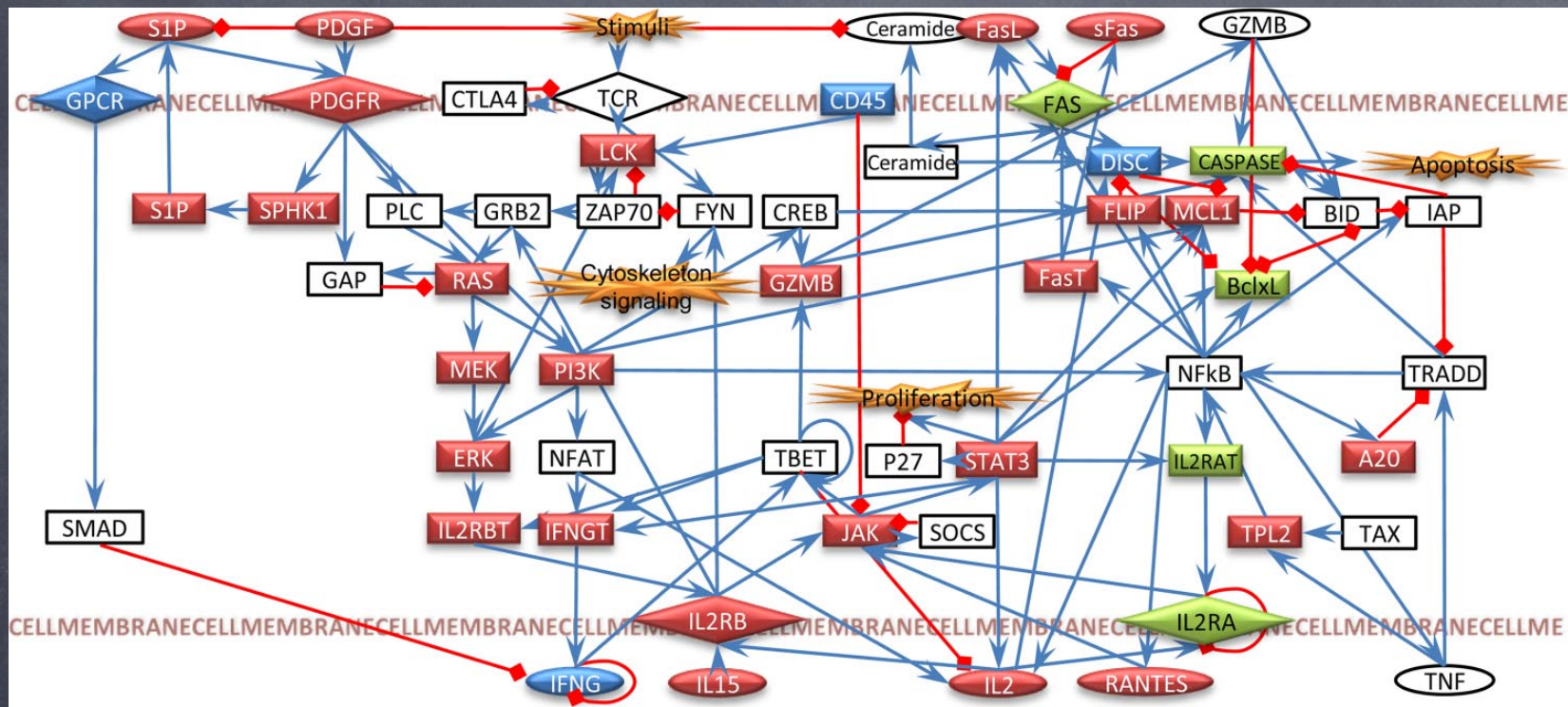
Largest "fluxes"

Noisy landscapes



# A Mammalian Example

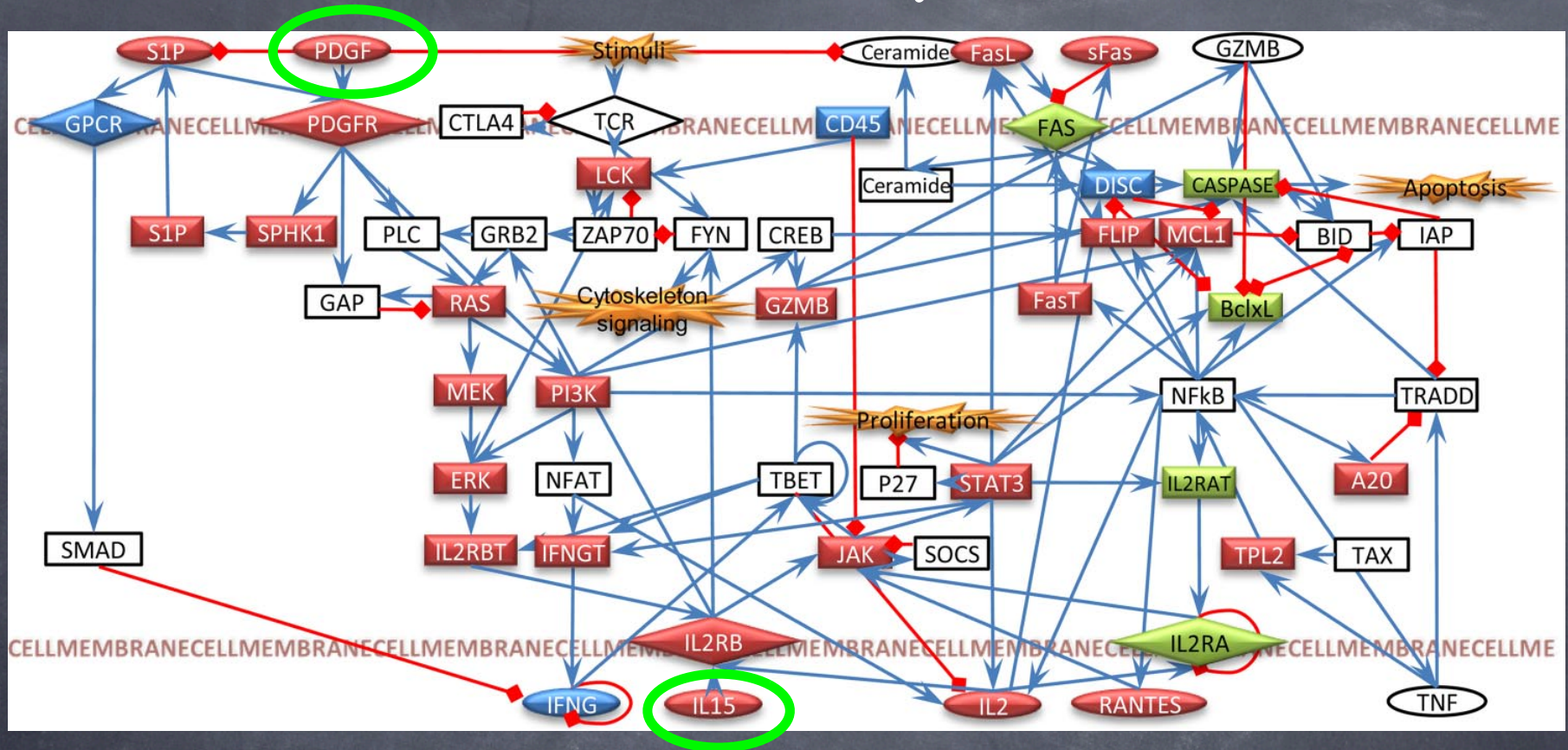
## Survival signaling in Large Granular Lymphocyte Leukemia



- ➔ Extensive literature search of Activation induced Cell Death in cytotoxic T lymphocytes
- ➔ All know deregulation of the process
- ➔ Boolean rules from literature

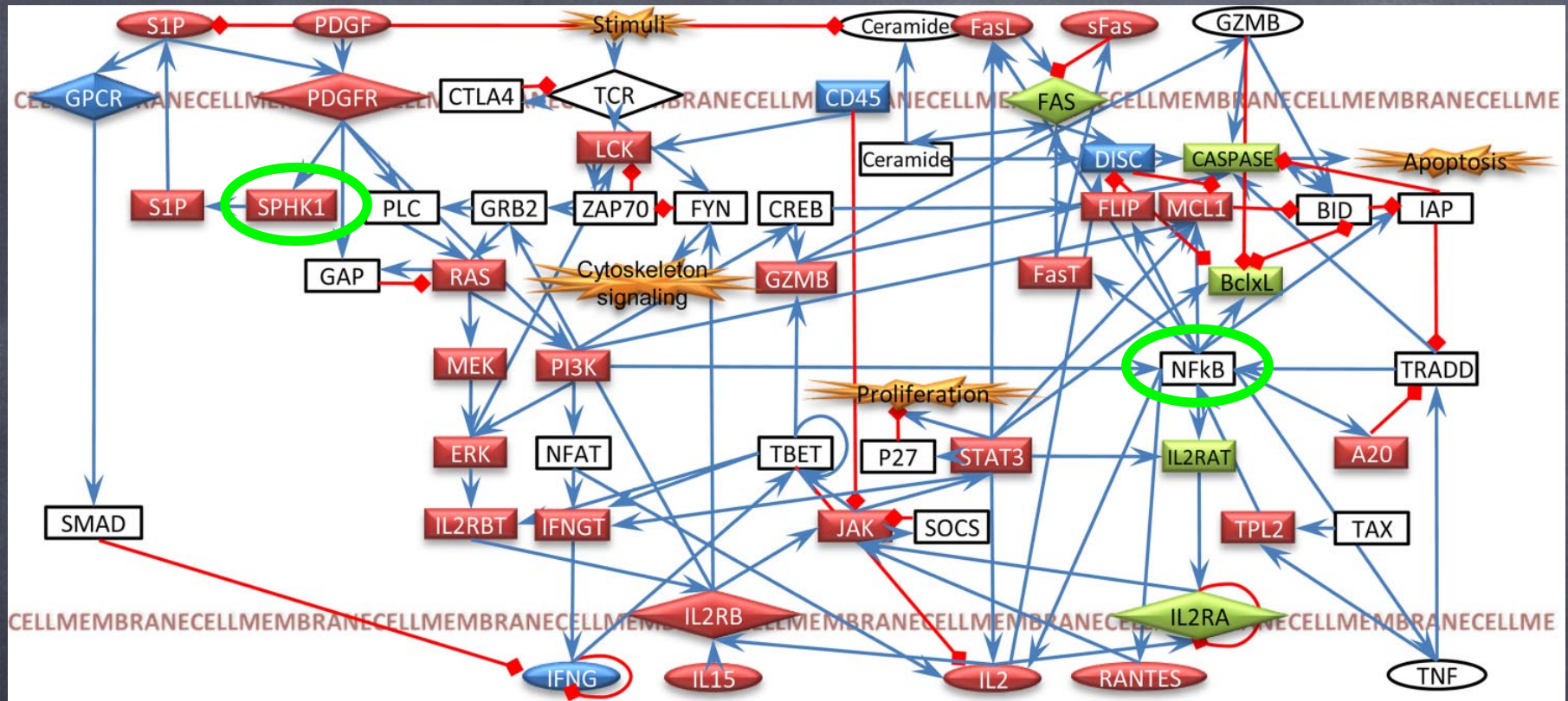
- Asynchronous update: a different way to model noise
- cell population response:
  - ➔ start from same initial state
  - ➔ different random update order

# Results, 1



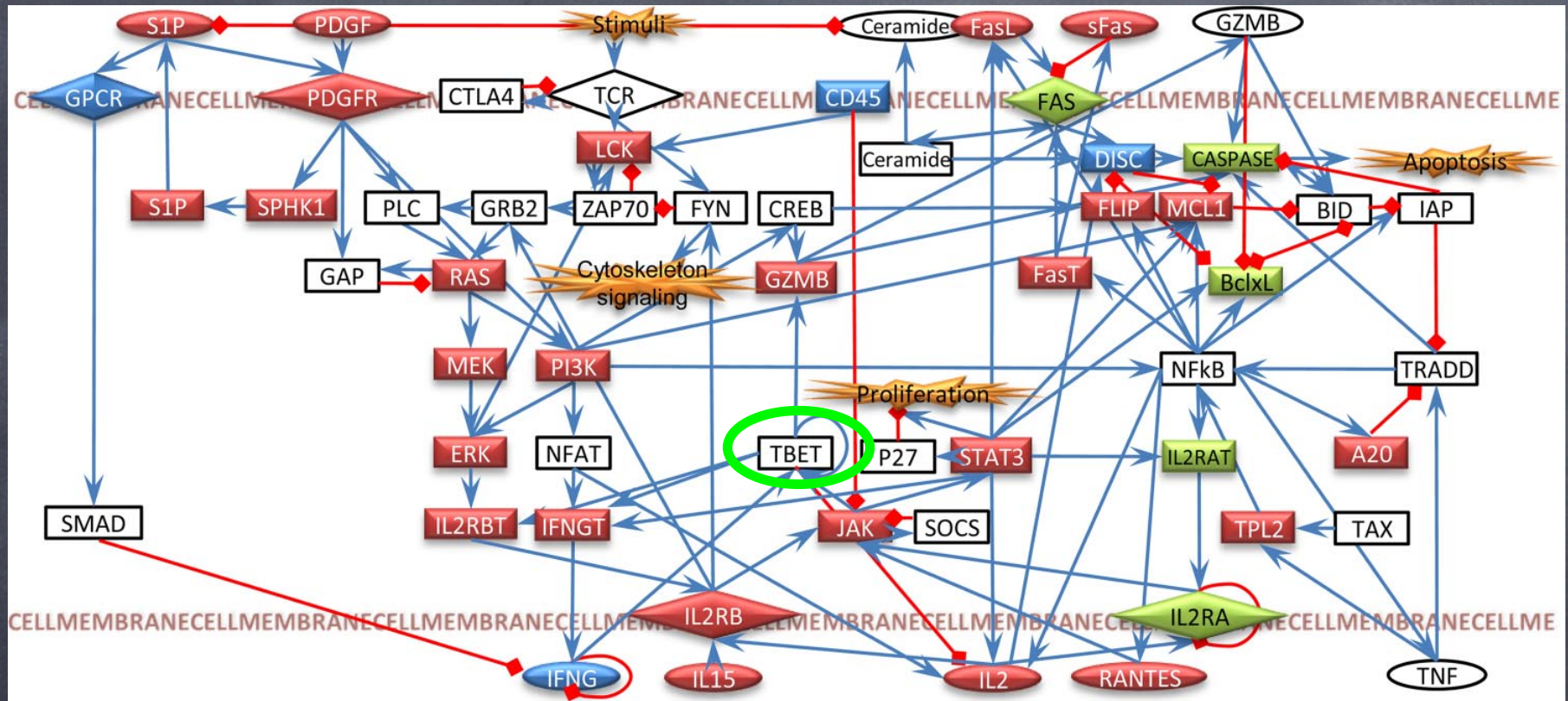
- Constitutive presence of IL15 AND PDGF reproduces all deregulation of apoptosis
  - experiment: increased PDGF in T-LGL sera
  - PDGF receptor inhibition makes T-LGL Peripheral Blood Mononuclear cells apoptotic, (normal ones do not mind!)

# Results, 2



- Key mediators of activation and AICD decoupling: NFkB and SPHK1 (Sphingosine Kinase 1)
- SPHK1 inhibition OR NFkB inhibition makes T-LGL Peripheral Blood Mononuclear cells apoptotic, (normal ones do not mind!)

# Results, 3



- TBET is predicted to be constitutively active in T-LGL
- TBET levels Peripheral Blood Mononuclear cells is 3.3 fold higher than normal PBMCs

# 6. Regulatory Models that Mimic Phenotype and Dynamics, Part II

- Cycles and their stability -

June 8

12 PM